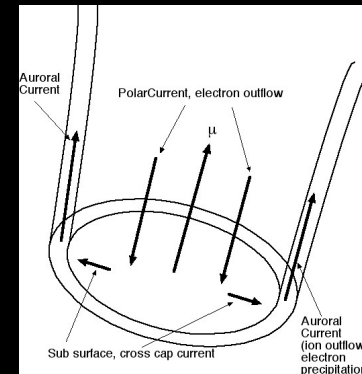
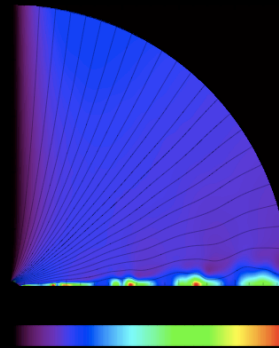
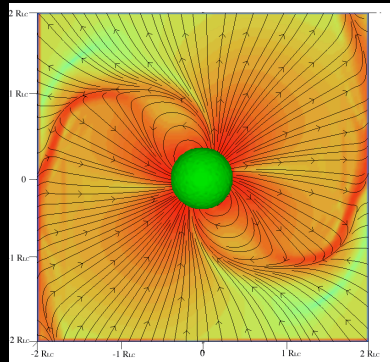
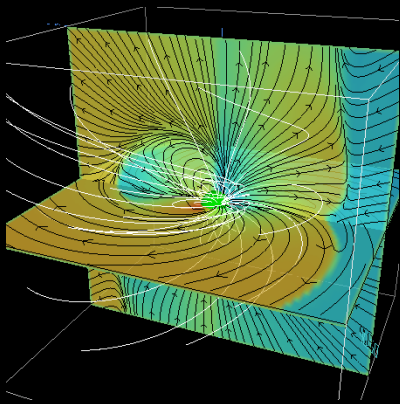


Pulsars: Problems and Prospects

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University of California, Berkeley



Collaborators: D. Alsop, E. Amato, D. Backer, P. Chang, **N. Bucciantini**, B. Gaensler, Y. Gallant, V. Kaspi, A.B. Langdon, C. Max, **E. Quataert**, **A. Spitkovsky**, M. Tavani, A. Timokhin

Follow the Energy: Spindown

Force Free Magnetosphere -

Spin down by EM torques

Magnetic energy dominant, non-vacuum, enough plasma for $\mathbf{E} \cdot \mathbf{B} = 0$

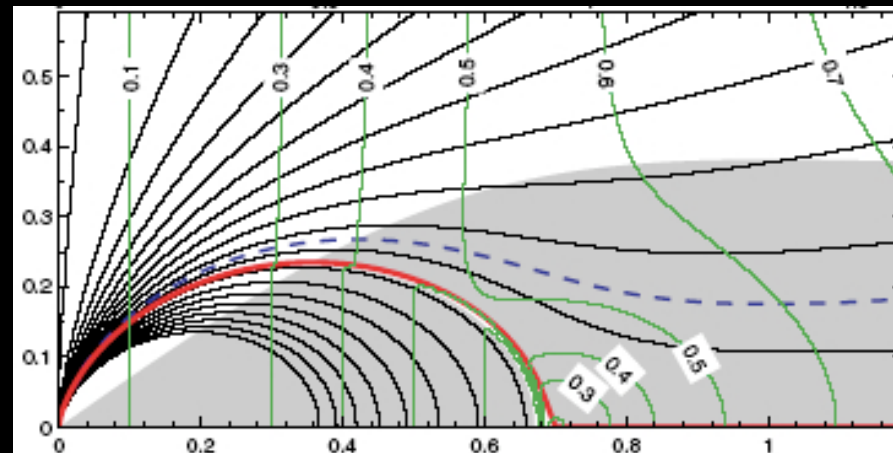
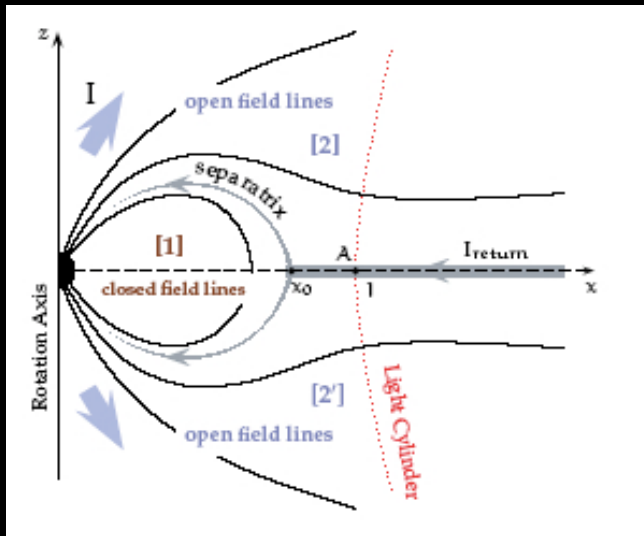
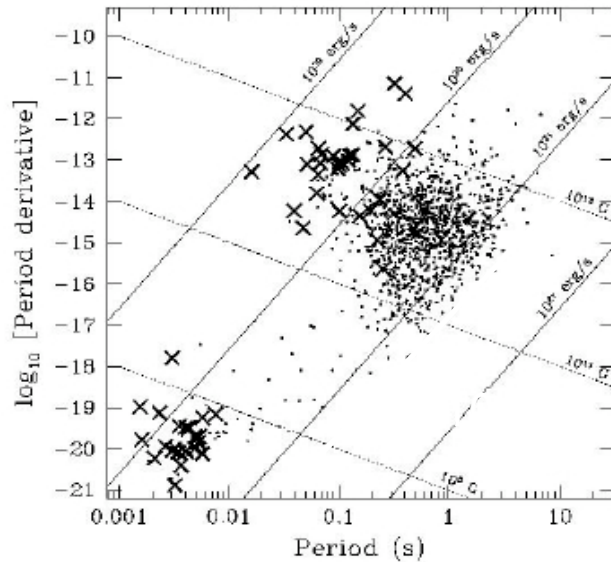
Contopoulos et al (99APJ), Gruzinov (05PRL),

Timokhin (06MN, 02-15): FF, aligned rotator,
steady state: $R_Y \leq R_L$

Komissarov 06MN rel MHD, McKinney 06 ApJ FF: aligned
rotator, evolutionary

Bucciantini et al 06MN, rel MHD, pressure driven flow,
aligned rotator, evolutionary: $R_Y \rightarrow R_L$

Spitkovsky 06ApJ: FF, evolutionary, aligned
& 3D oblique: $R_Y \rightarrow R_L$ (also kalpotharakos+09)

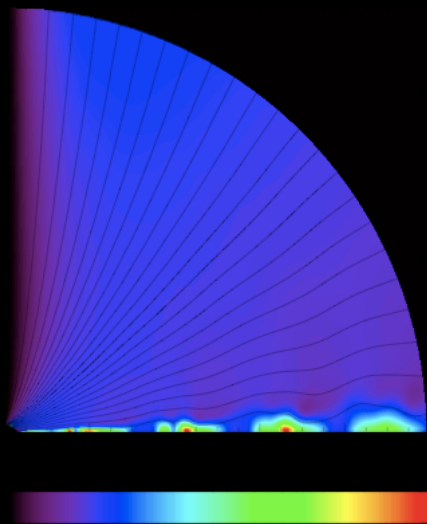


$$R_Y \leq R_L$$

$$n = \frac{\Omega \ddot{\Omega}}{\dot{\Omega}^2} = 3 + 2 \frac{\partial \ln \left(1 + \frac{R_L}{R_Y} \right)}{\partial \ln \Omega}$$

$R_Y/R_L < 1$ increases torque because of more open field lines and larger Poynting flux for same R_L

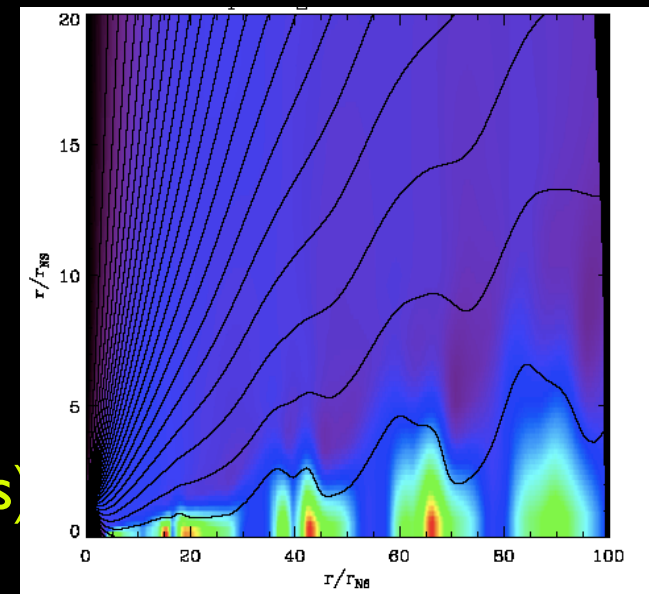
IF R_Y/R_L decreases with decreasing W , $n < 3$;
average R_Y/R_L must decrease on spindown timescale, since $2 < n < 3$



Bucciantini et al 06

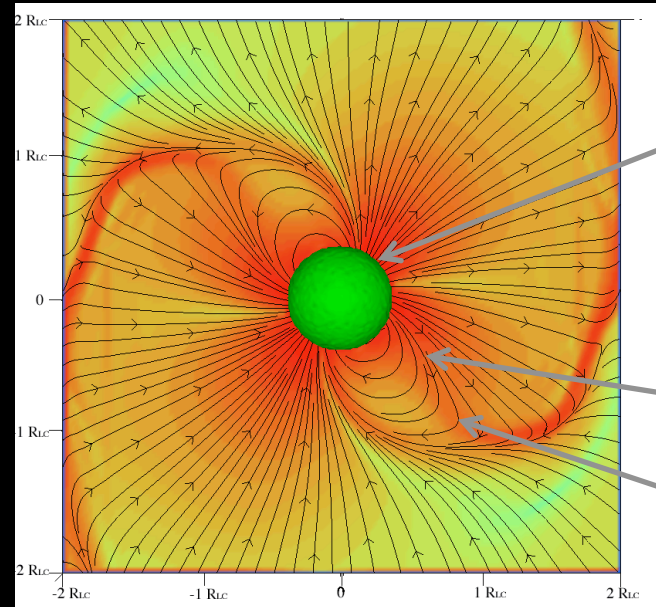
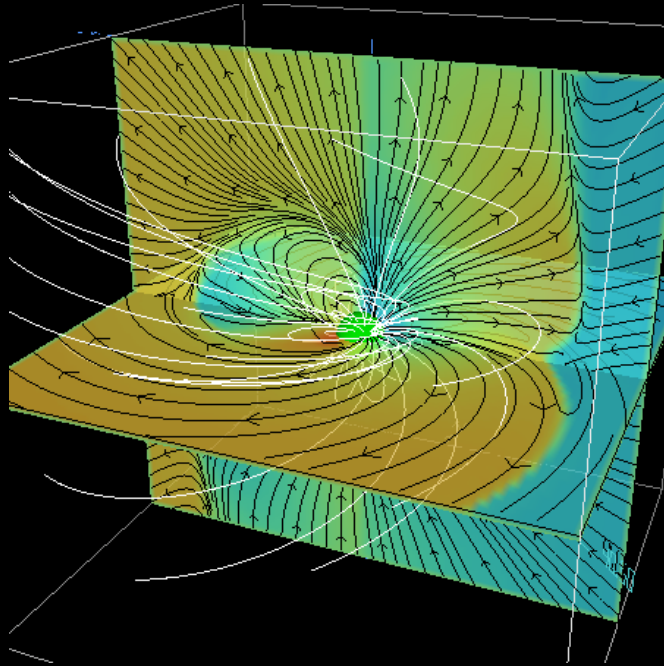
“Average” with respect to plasmoid emission, torque fluctuations
($\delta T/T \sim 10-30\% \sim \text{obs}$)

Spindown biases fluctuations toward increasingly open flux??



Aligned Rotator IS like the oblique object (spindown)

Spitkovsky's (2006) oblique force free rotator (ApJL)



Polar Gap

Slot Gap

Outer Gap

Total Current

Field Lines (with real open flux)

$$\dot{E}_R = -I\Omega\dot{\Omega} = k \frac{\mu^2 \Omega^4}{2} (1 + \sin^2 i), \quad k = 1 \pm 0.1$$

$$i = \angle(\mu, \Omega)$$

Gaps = local zones
of charge density $< G_j$,
Parallel $E \neq 0$

Acceleration along B
→ beamed photons,
rotation → lighthouse

Force Free model has no gaps, no parallel accelerator

Implications for Emission:

- Polar cap/flux tube size and shape - noncircular shape, center from displaced magnetic axis - polarization - no need to invoke non-dipole B?
- Electric current magnitude and sign - return currents both spatially distributed and (mostly) in thin sheet - if dissipation regions (“gaps”) have parallel potential drops small compared to total magnetospheric voltage,

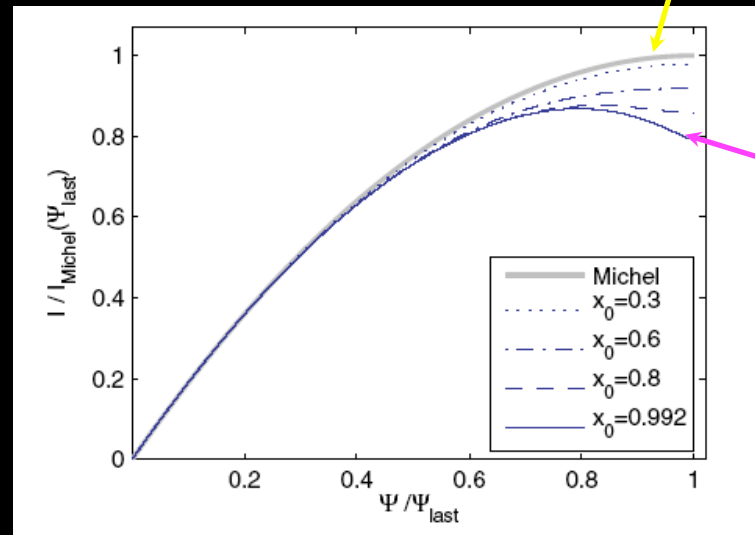
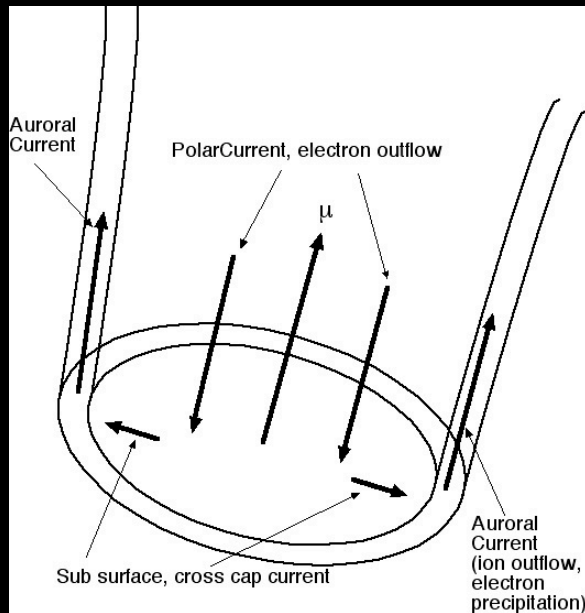
$$\Phi = \sqrt{\frac{\dot{E}_R}{c}} = 4 \times 10^{16} \text{ Volts} \left(\frac{\dot{E}_R}{10^{38.7} \text{ erg/s}} \right)^{1/2} \propto L_{\text{radio}}, L_{\gamma}(\text{large } \Phi)$$

electric current in and outside gaps is known, averaged on magnetosphere transit time ($\sim P/\pi$) - electric currents of gaps/emission sites must fit into magnetospheric circuit - or force free magnetospheric model is wrong - but energy all in field, hard to be non-FF

- Location of return current layer determined - realistic site/physics for outer magnetosphere beaming models of high energy emission)

Known Current - Huge Effect on E_{\parallel} ?

Aligned rotator for clarity



Polar current contained within
distance from magnetic axis, $j \neq \text{const}$

Cartoon - all models have charge $\varpi = \left(\frac{\psi}{\pi B_{pole}} \right)^{1/2}$, ψ = Magnetic flux density = GJ, polar current density = constant

⇒ “small” E_{\parallel} ($\sim 10^8$ V/m); same true for outer gaps
(geometry different, electrodynamics \sim same)

Effect of Current on E_{\parallel} (continued)

Existing models (RS, FAS, SAF, MT): starvation E_{\parallel} extracts a beam -

Beam Charge Density almost equals GJ : current = constant -
small E_{\parallel} - $\sim 10^8 \text{ V/m}$, $DF \sim 10^{12} - 10^{13} \text{ V}$

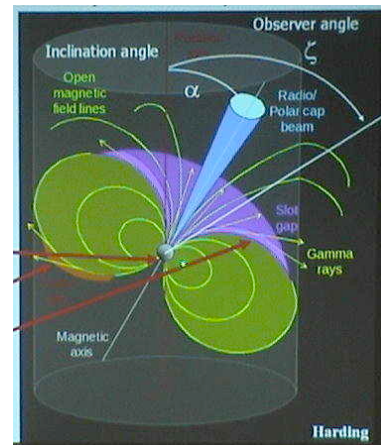
***local electrostatic tail wags
the magnetospheric dog!***

Same issue for outer gaps on open field lines:
starvation gap models (steady or unsteady) produce
magnetospheric charge density, not current density,
but all energy in current!

phenomenological models of data all based on such
anti-energetics ideas

Magnetosphere sets time average j_{pc} to be the Force Free current:
close to monopole

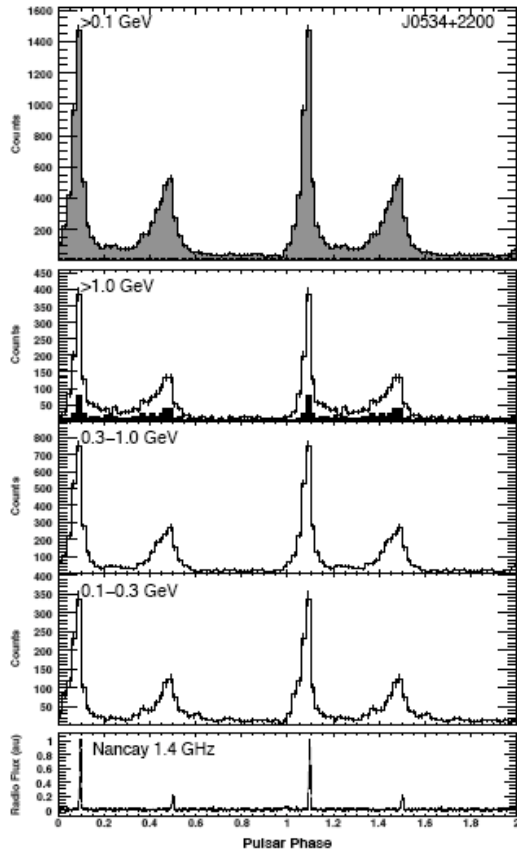
Like a vacuum gap, but $E_{\parallel} = 0$ at crust surface



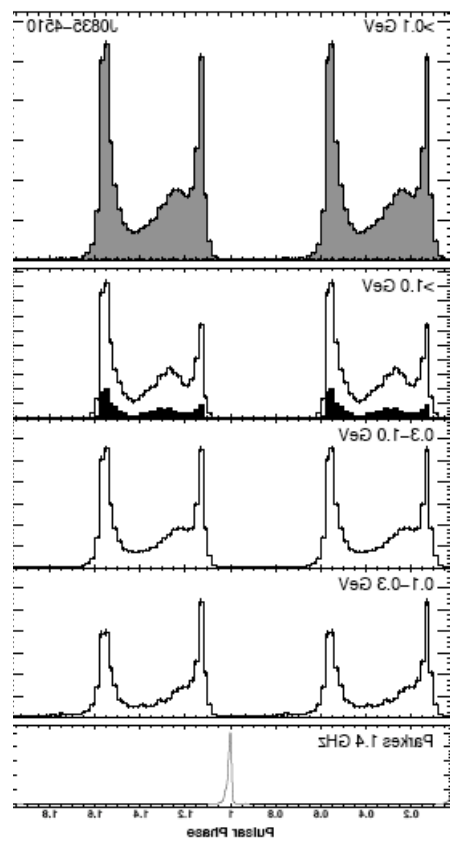
Gamma Ray Efficiency



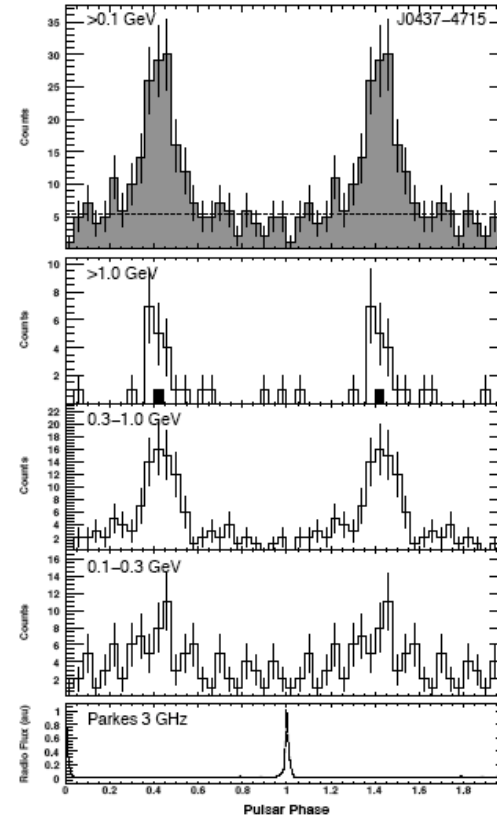
Crab, P=33msec



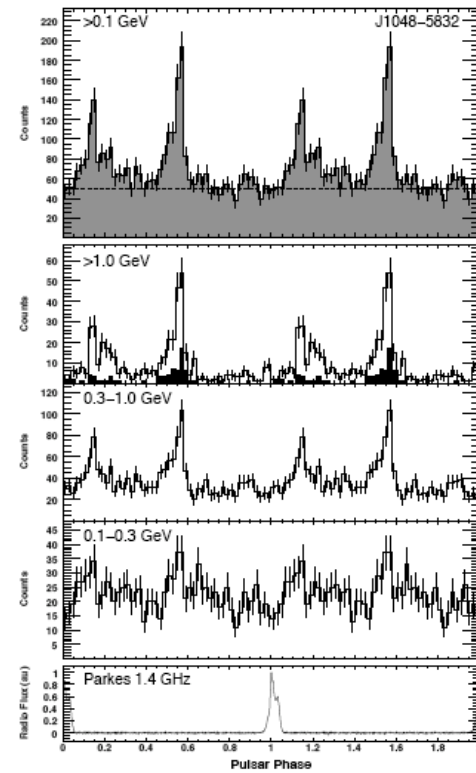
Vela, P=89msec



J0437, 5.76msec



J1048, 124msec



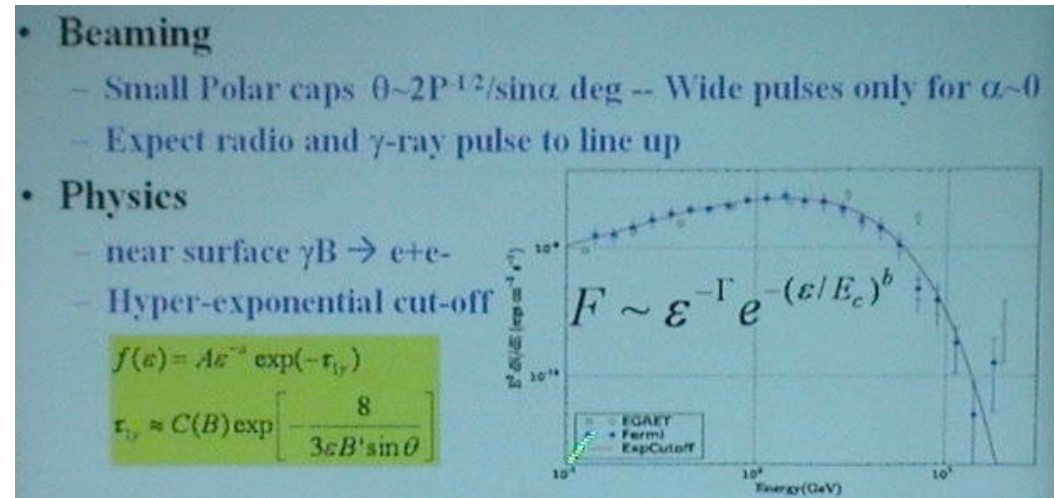
A Few Gamma Pulsars (46 seen by FERMI-LAT)

Most are double peaked, wide separation in rotation phase

Gamma Ray Tests of Existing Gap Models

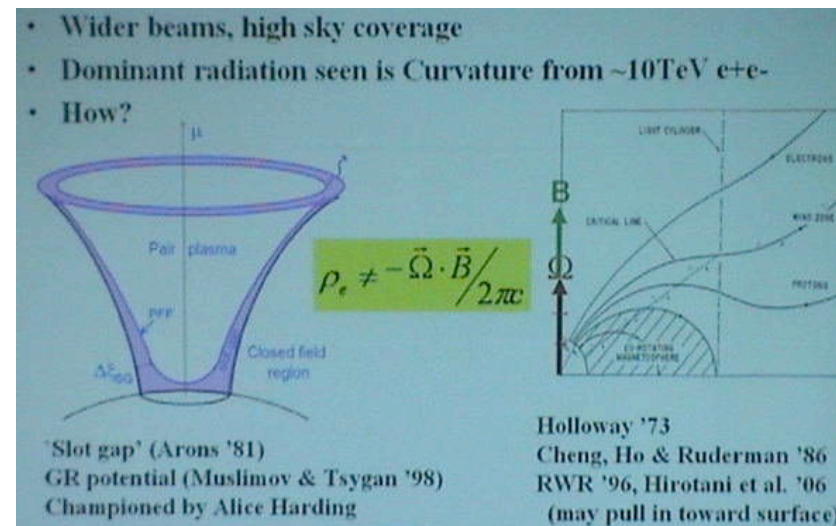
Gamma Rays Not from Polar Cap

Super exponential cutoff rejected:
 $b > 1$ rejected at 16σ

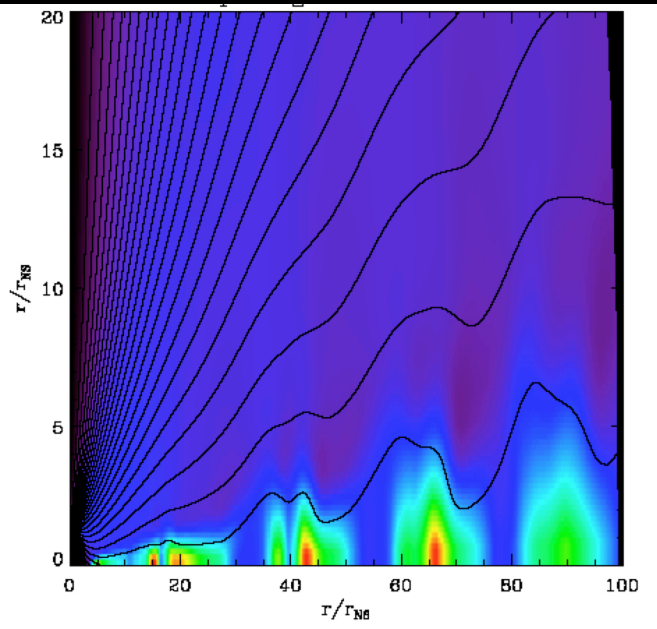


Beamed γ from high altitude
 more promising – tradition
 has $E_{||}$ from starvation,
 quasi-vacuum “gaps”

Slot gap fragile to mild magnetic
 anomalies, gravitational bending
 of photon orbits causes pairs to fill
 gap; Outer gap has physics inconsistent with FF magnetosphere

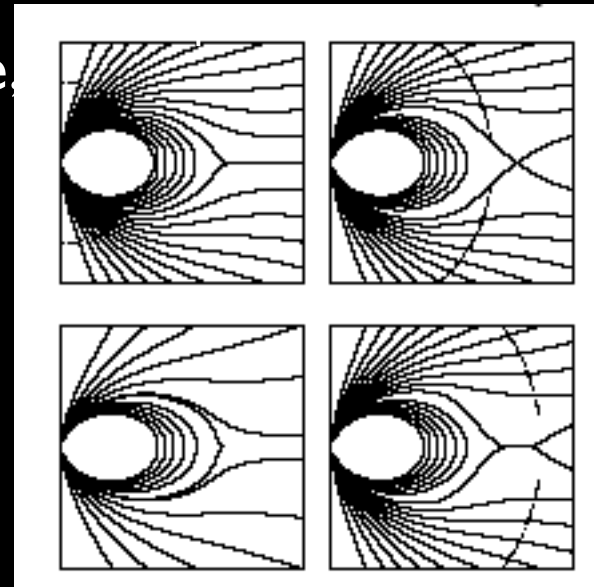


Prospect: Time Dependent Reconnection/Return j



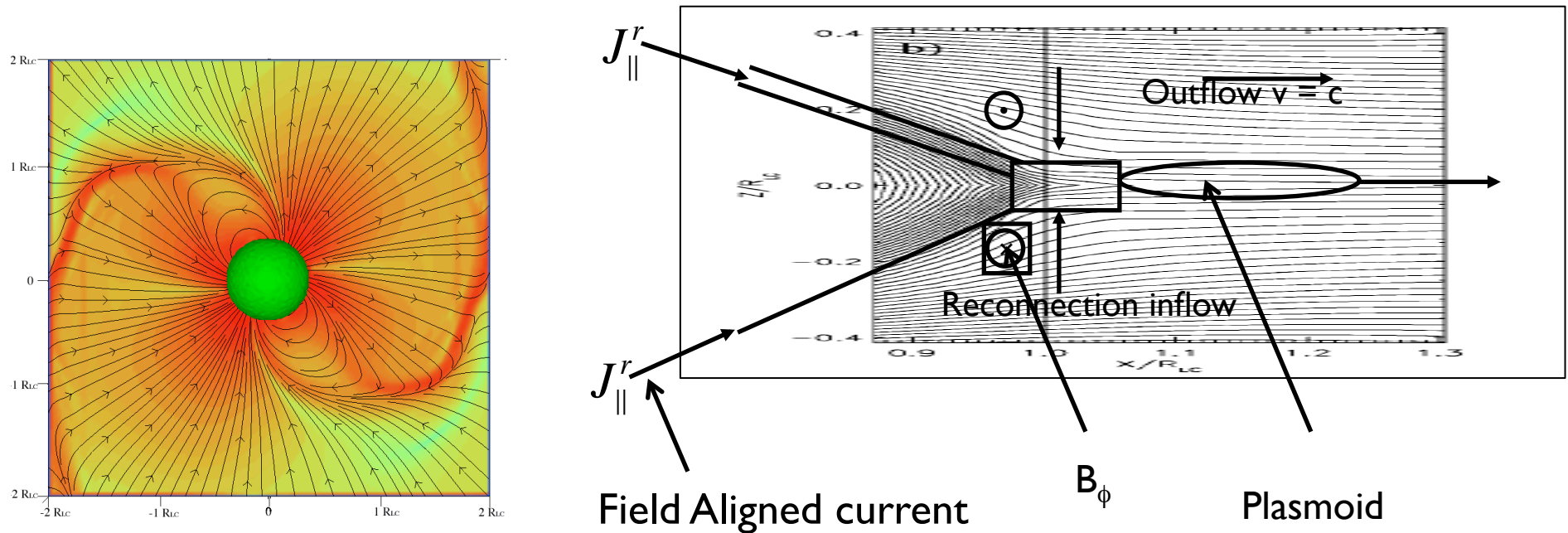
Sporadic X-Point, Plasmoid formation
occurs continuously

Pairs all come from pole
on open field lines
Sporadic reconnection
moves plasma across
separatrix
non-corotation, time
variable E at all times



- Plasma, j flow to star in thin separatrix layer - dynamics in Kinetic Alfvén waves, boundary layer E_{\parallel} - replaces outer gap
- Space charge in boundary current alters polar acceleration(!) enhances pair creation (?)
- Kinetic Alfvén wave E_{\parallel} extracts ion return current
- Torque fluctuations, limit cycles built in (drifting subpulses)

Acceleration in Current Sheets – New Work (in progress), with A.S.



Current Sheet = “Kinetic Alfvén Wave”, thickness $\sim c/\omega_p$

$$\mathbf{E} = \mathbf{E}_{\text{perp}} + \mathbf{v} \times \mathbf{B} + \mathbf{E}_{\text{parallel}}$$

$$E_{||} = \frac{4\pi}{\omega_p^2} \frac{DJ_{||}}{Dt}$$

Vacuum gap (starvation) not in picture, particle inertia good enough to provide “resistance” in large inductance circuit, voltage $\rightarrow \Phi$

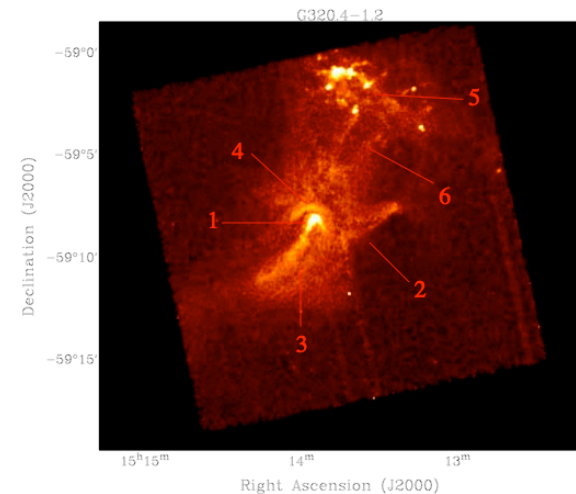
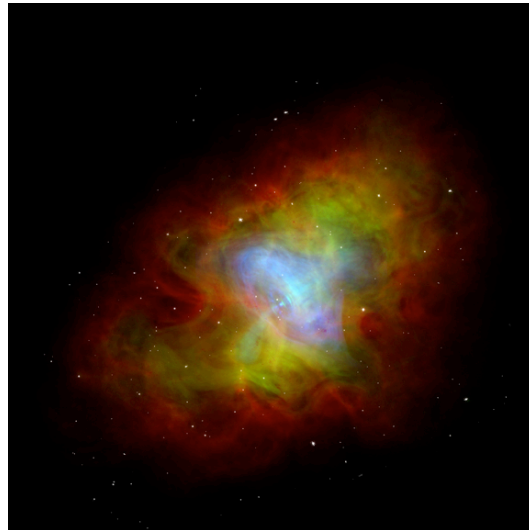
Follow the Mass Loss: From Whence all the Pairs?

Pulsar Wind Nebulae: Nebular Synchrotron requires particle injection $\dot{N}_{\pm} \gg \dot{N}_{GJ} = c\Phi/e$

PAIR PROBLEM

X-Rays: current injection rate (compact, strong B nebulae - Crab, G54,...)
measured rates \sim existing (starvation) gap rates $\kappa_{\pm} = \dot{N}_{\pm} / \dot{N}_{GJ} \leq 10^4$ pairs/GJ

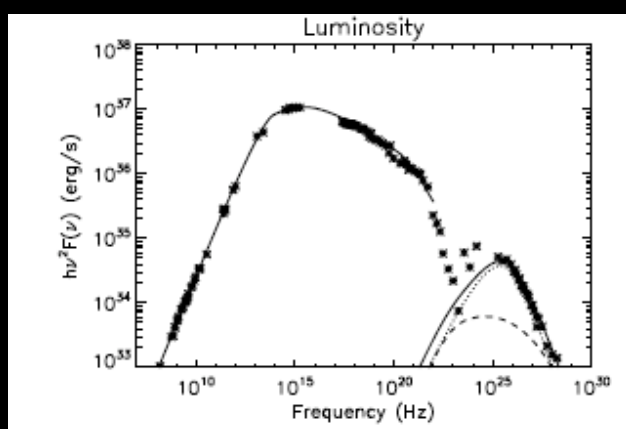
Radio measures injection rate averaged over nebular histories. rate $> 10^6$



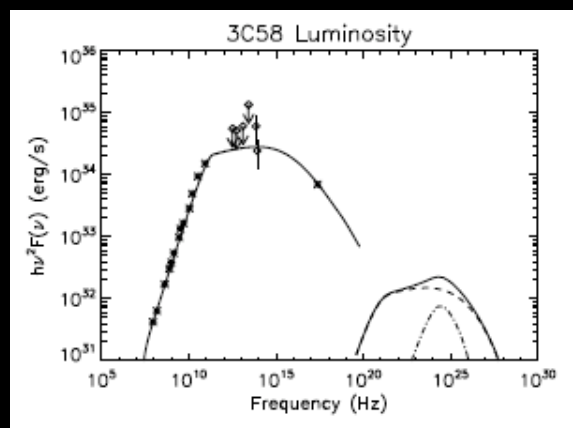
Low $\sigma = B^2/8\mu_0 m_{\pm} c^2 n_{\pm} \Gamma_w$ at termination $\rightarrow \Gamma_w = e\Phi/2m_{\pm} c^2 \kappa_{\pm}$

PWN Name	κ_{\pm}	Γ_w	$F_{\text{init}}(\text{PV})$	Age (yr)
Crab	$> 10^6$	5×10^4	100	955
3C58	$> 10^{5.7}$	3×10^4	15	2100
B1509	$> 10^{5.3}$	1×10^4	121	1570
Kes 75	$> 10^5$	7×10^4	22	650

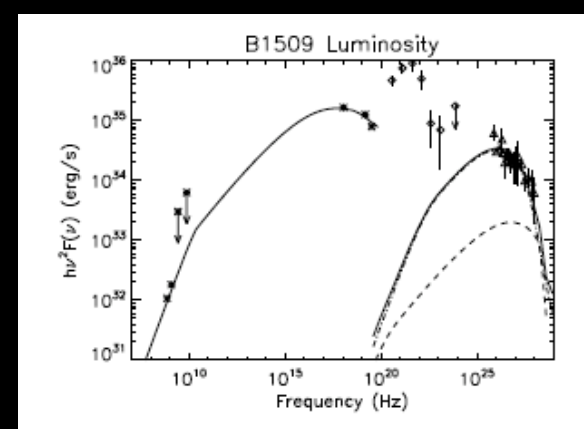
From one zone evolutionary model of observed spectrum including radio
(with Bucciantini, Amato) – injection spectrum convex, $\gamma^{-1.5} \rightarrow \gamma^{-2.3}$



Crab



3C58

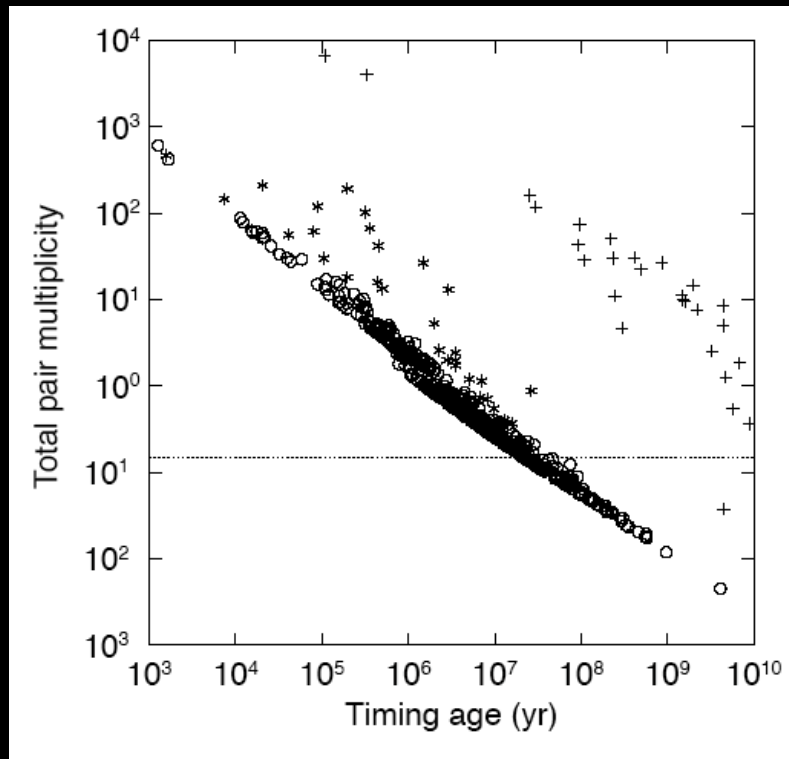


PSR B1509/MSH 15-52

Why so many Pairs (continued)

Pulsar death line ($\Phi = \sqrt{\dot{E}_R / c} \approx 10^{12}$ V) models need dense ($E_{\parallel} = 0$) pairs over all P, \dot{P} space

Starvation electric field polar caps (charge density controls current) do make a few pairs at low voltage (plenty at high Φ), but not dense - shorting out electric field not clear - more pairs needed (or FF-MHD not applicable) - same lesson as from PWNe



Many (not all) radio emission ideas need dense (large multiplicity) pairs
All transfer effects need dense pairs - something is missing (not non-dipole fields!)

Hibschman & JA 01

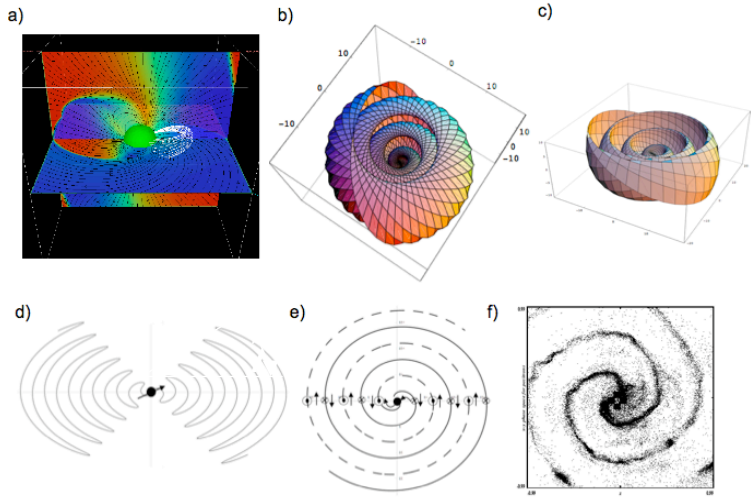
Likely flaw: All models assume density $\gg GJ$ in current carrying plasma have zero parallel E - NOT TRUE – aurora

Shorting out E_{parallel} at surface of first pair creation assumed by everyone, good idea (?) in steady flow, Not so in unsteady flow

- Current + pairs becomes time dependent (?), averages to FF (GJ , Alber et al, Levinson, others), electric field averages to small starvation (?) value – PC heating? Large E_{parallel} over greater length: more pairs (?)

(Timokhin & JA PIC + Monte Carlo hybrid)

Prospect: Wind Structure, dissipation and (?) emission: low σ at TS

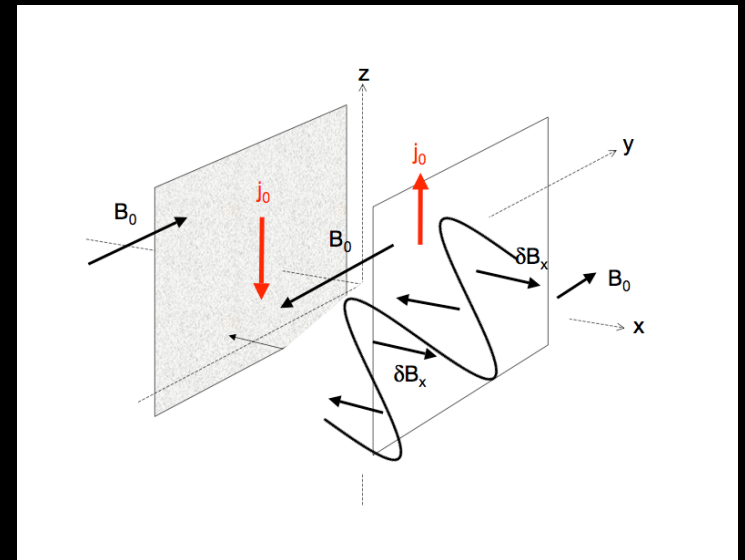


Oblique rotator:
striped wind ($-\iota < \lambda < \iota$)
Current sheets blow
out at speed c
Sheets dissipate,
 $R_L \ll r \ll R_{\text{shock}}$

Two Stream (Weibel-like)
Instability of neighboring sheets
Anomalous B diffusion at Bohm rate

Dissipation of Stripes (low σ) at $r \ll R_{\text{TS}}$
Radiation from stripes (pulses?)

Asymptotic wind \longrightarrow aligned rotator?



Other current flow instabilities in current layer lead to similar anomalous resistivity & stripe decay (collisionless tearing mode, drift kink instability: “reconnection”, although detailed X-point dynamics likely inhibited): Striped component of toroidal field converted to kinetic energy of flow at $r \sim 0.01-0.1 R_{TS}$ –

REQUIRES LARGE MASS LOADING, $\Gamma_w < 10^{4.5}$

Runaway Beam in Current Sheet: DIFFUSION COEFFICIENT PROPORTIONAL TO p^2 , current carriers become “runaways”:
 gain energy faster in resistive electric field than scattering causes loss, current becomes a beam, energy/particle $\rightarrow e\Phi$ –
 large fraction of spindown energy loss carried in current sheet, acts as a linear accelerator (weak synchrotron losses)

Flow upstream of termination shock is low σ , pairs + high energy beam carrying comparable amounts of the kinetic energy flow

Beam composition: electrons ($\Omega \cdot \mu > 0$)

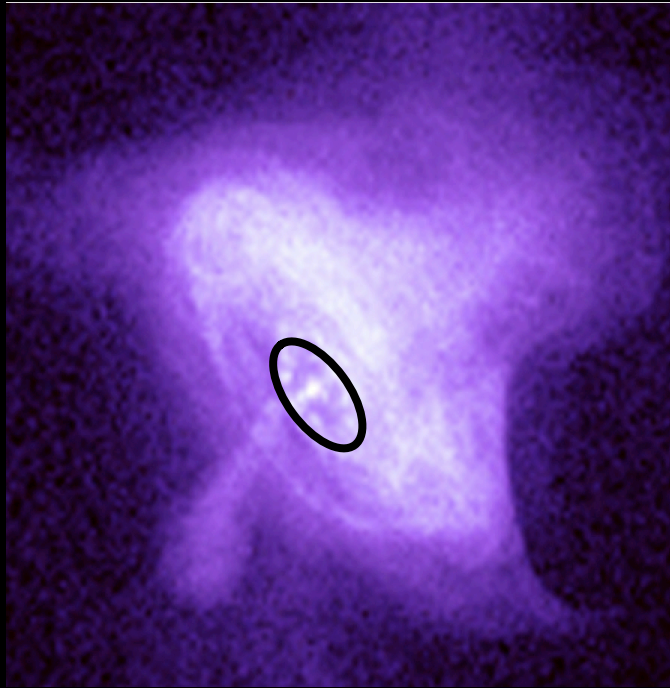
positrons (+ heavy ions drawn up from surface): ($\Omega \cdot \mu < 0$),

proportion depends on reconnection dynamics at Y line, partition uncertain

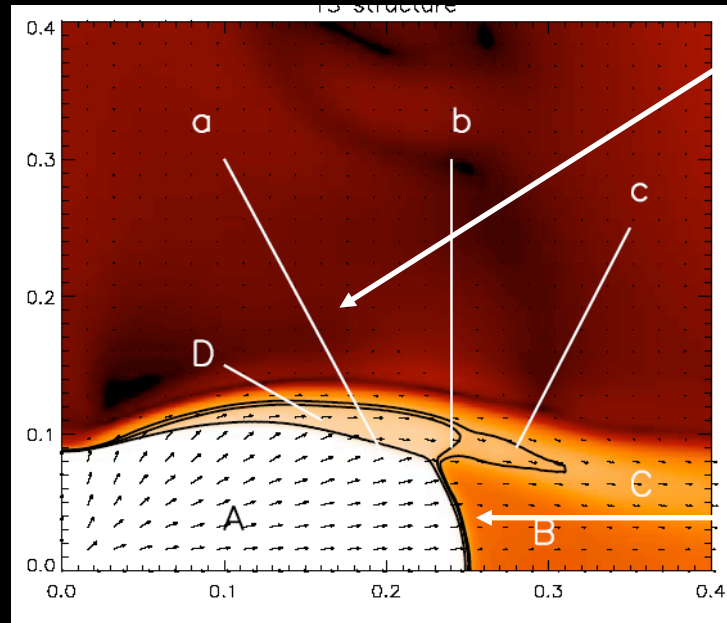
Beam component has large inertia/particle,

$$\gamma \approx q_{\text{beam}} \Phi / m_{\text{beam}} c^2 \quad r_{\text{Larmor}} \approx R_{\text{shock}}; L_{\text{beam}} \approx L_{\text{spindown}} (??)$$

Termination Shock = Magnetic Sandwich



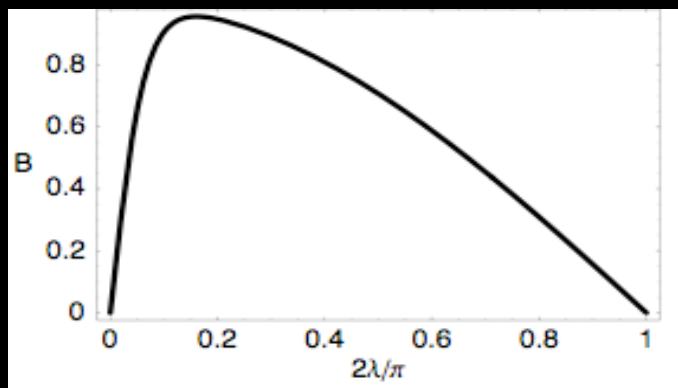
Termination Shock Location



High density
pairs, mildly
magnetized
shock

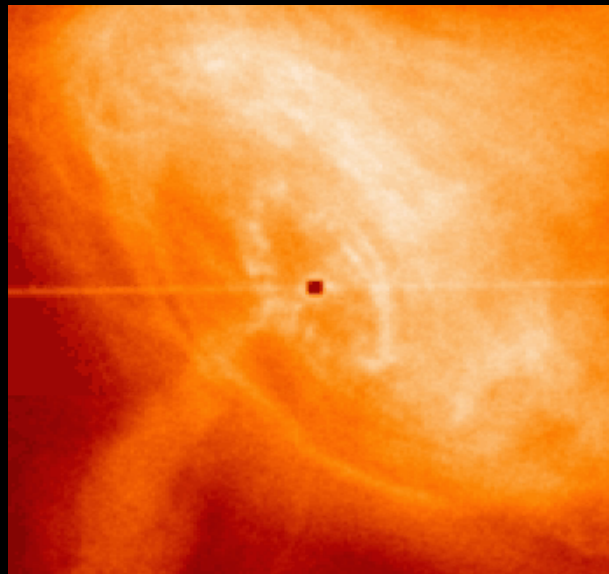
Low density
pairs, beam,
unmagnetized
shock

Termination Shock Structure
(from del Zanna et al 04)

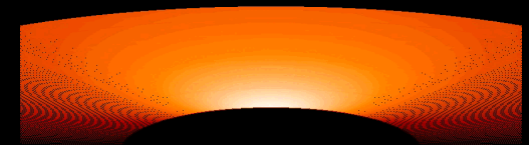


B strength with latitude -
Unmagnetized in equator

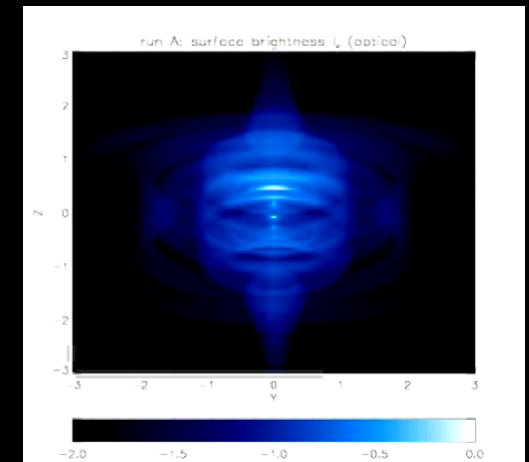
J.Arons: HEPROII 2009



Chandra Movie



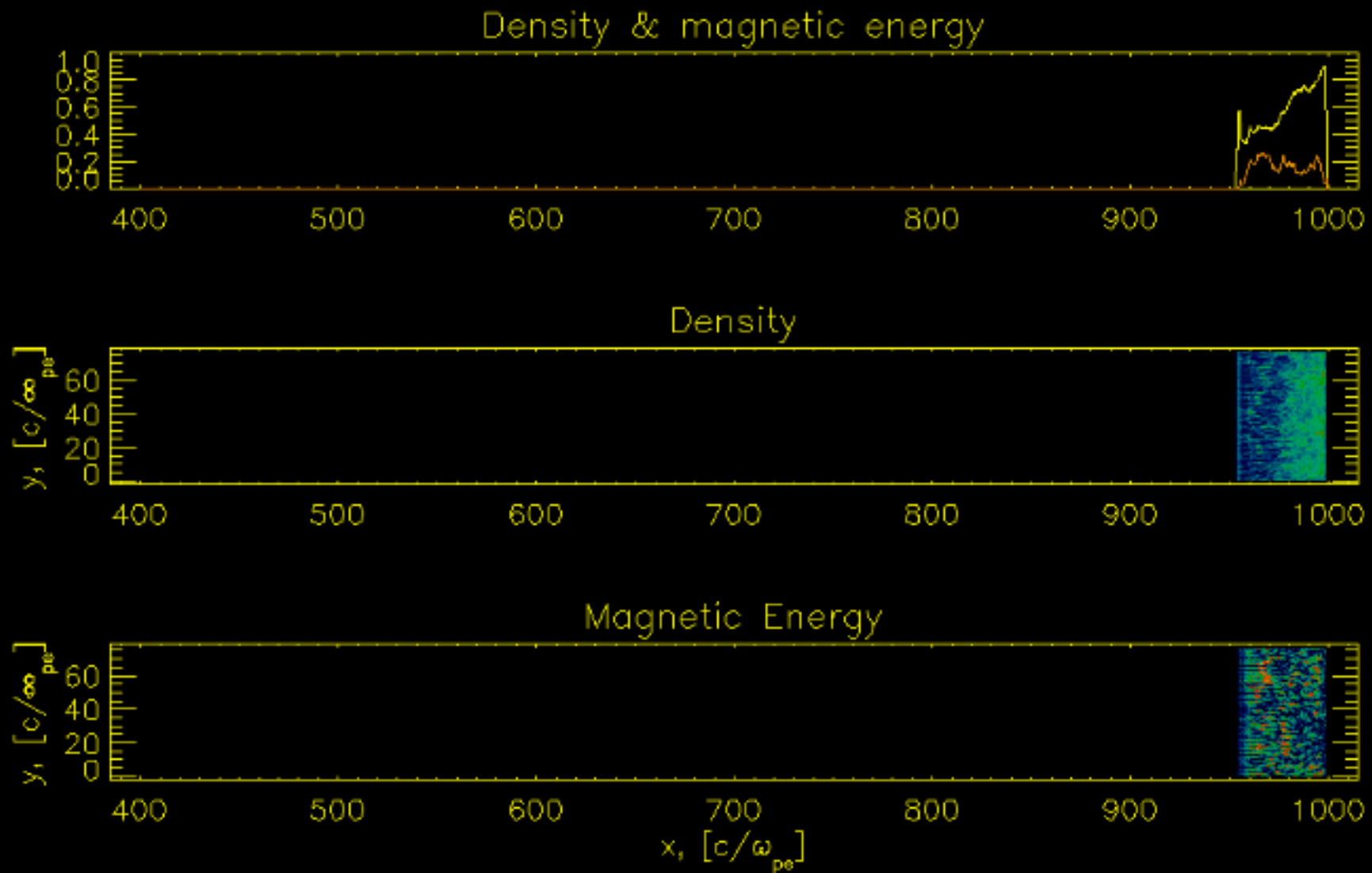
Equatorial beam compressions Movie (AS+)



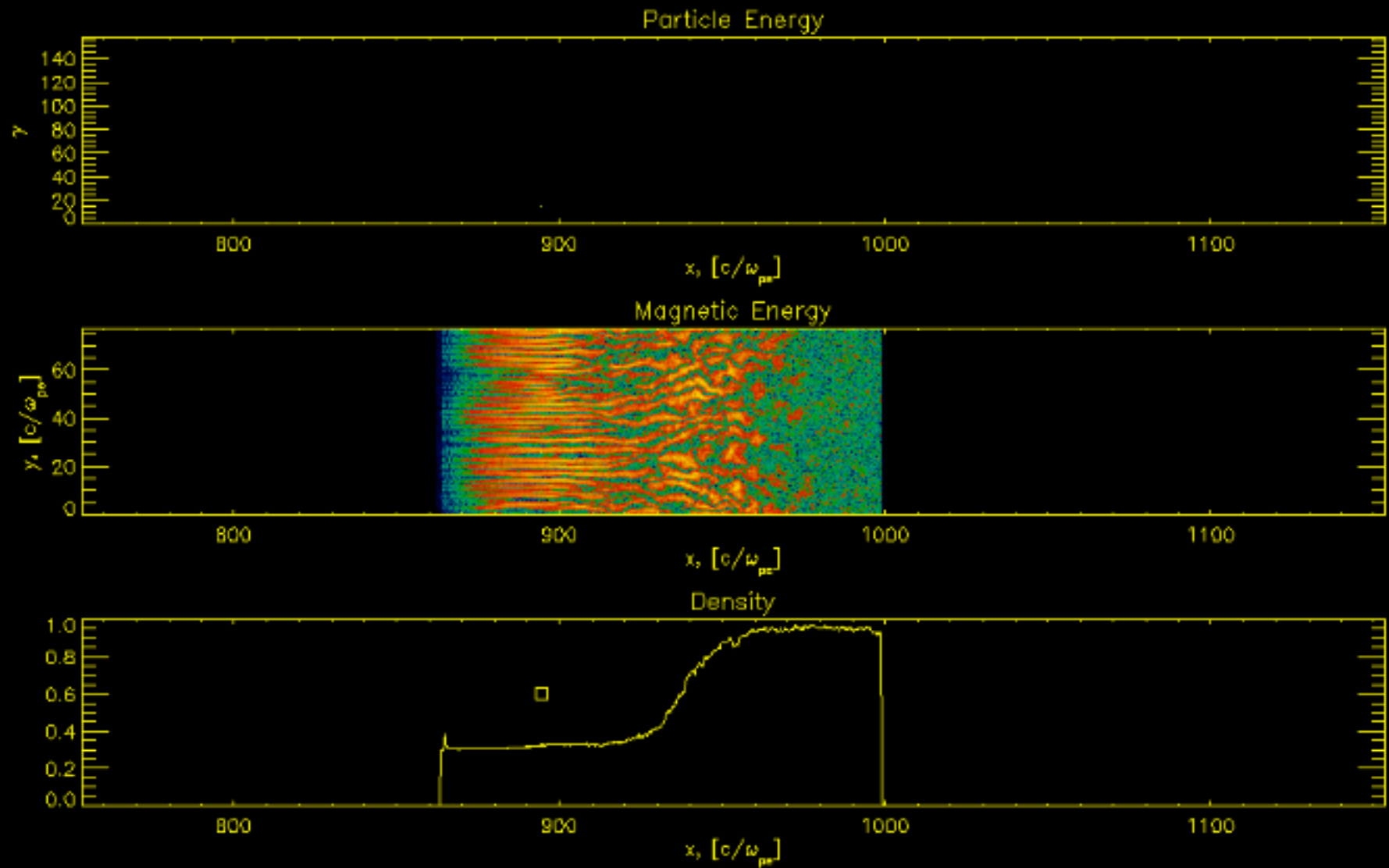
MHD Shear and Vorticity Instability Movie (SK+)

Unmagnetized shock Movie (Spitkovsky 08)
PIC Simulation of Weibel turbulence mediated shock

2.5D relativistic PIC, electrons-positrons, $B_0 = 0$, $\Gamma=15$; 3D (Spitkovsky & JA) similar



Movie - Trace particles that end up in the tail - scattering weakens at large γ , particles lost to tail.



Large simulations (50,000x800 cells, 5000x80c/ω_{p±})- suprathermal particles (Fermi acceleration) well developed

Density, $t=8400/\omega_p$
B^{1/2}, $t=8400/\omega_p$

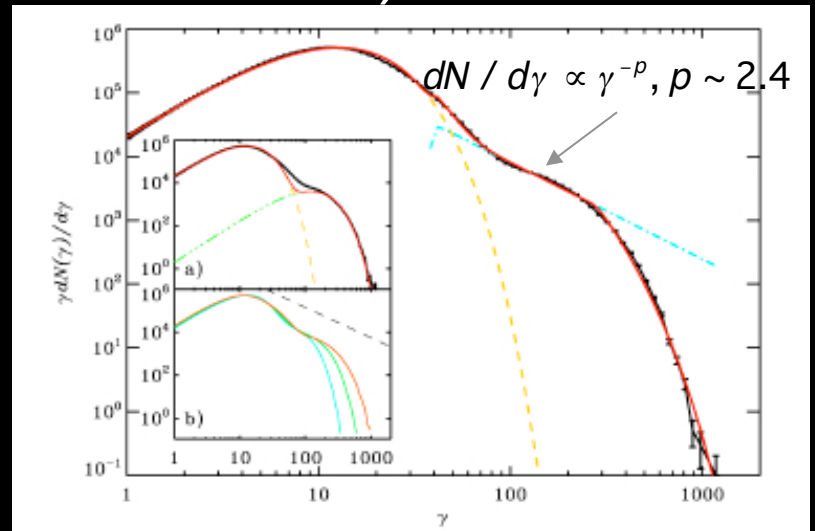
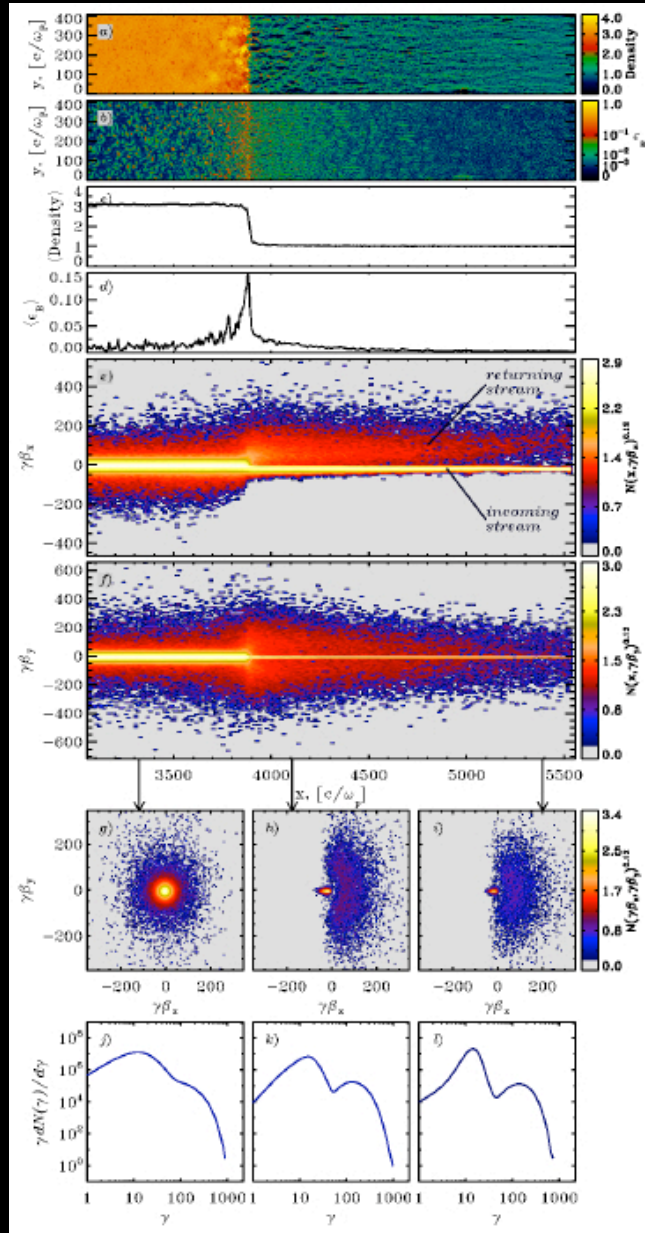
ID density, B^{1/2}
 $t=8400/\omega_p$

P_{flow}-x

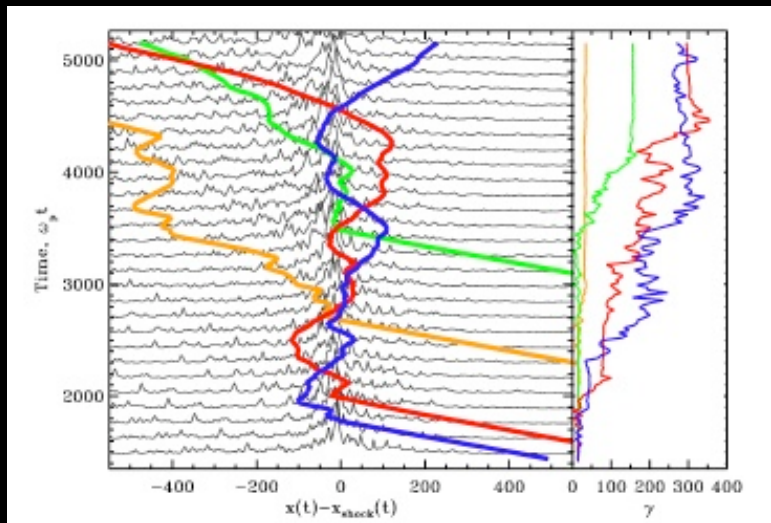
P_{perp}-x

P_{flow}-P_{perp} slices

Particle spectra
in slices



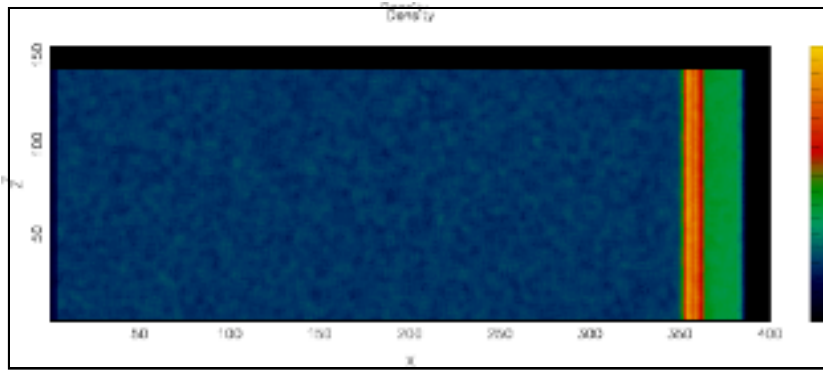
Downstream particle spectra: Maxwellian +
exponentially cutoff power law (biMaxwellian,
growth of power law component)



Labeled particles gaining energy

Magnetized Transverse Pair Shock (higher latitude):

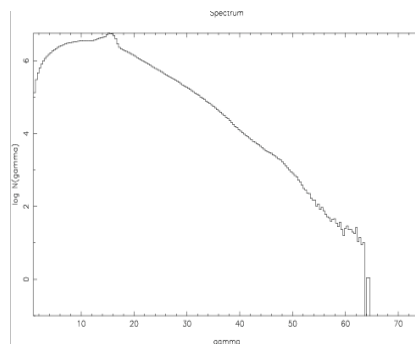
Pairs, unidirectional B, 3D, colliding shells, $\sigma = 0.1$ 3D Phase space



Density in B-v plane Movie

Complete Thermalization – rapid
relativistic synchrotron emission and self-absorption
(synch thermalization \sim BH disks, but collective) -
true for all superluminal Θ_{BN}

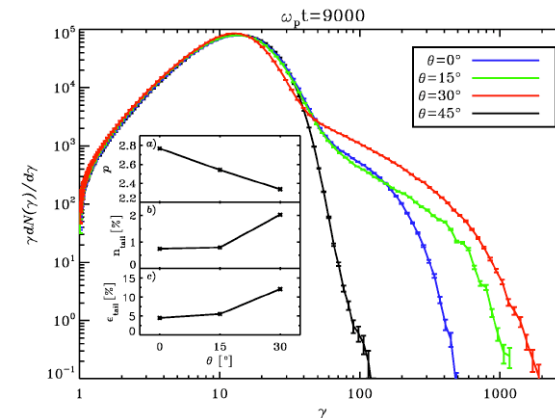
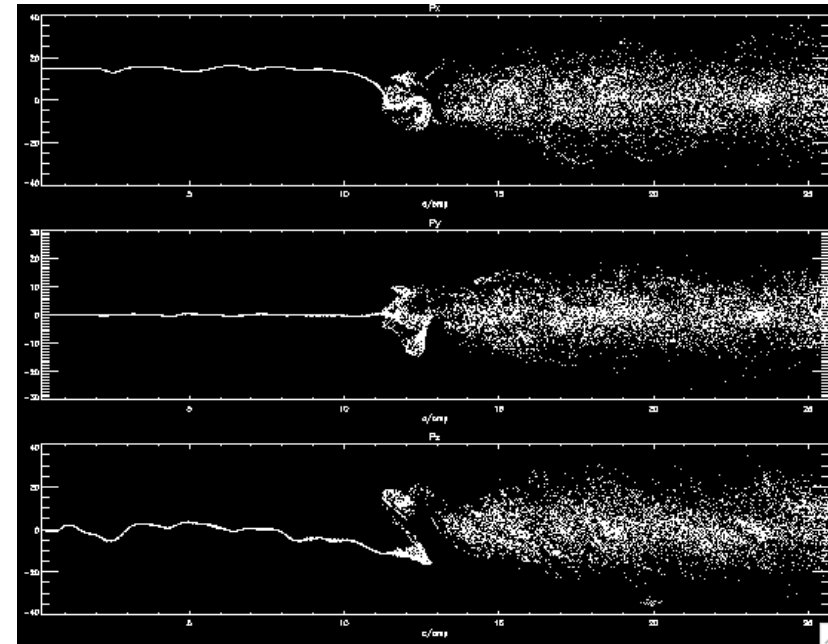
Log f(E)



P_{x-x}
 $<v_x$

P_{y-x}
 B_0

P_{z-x}
 E_0

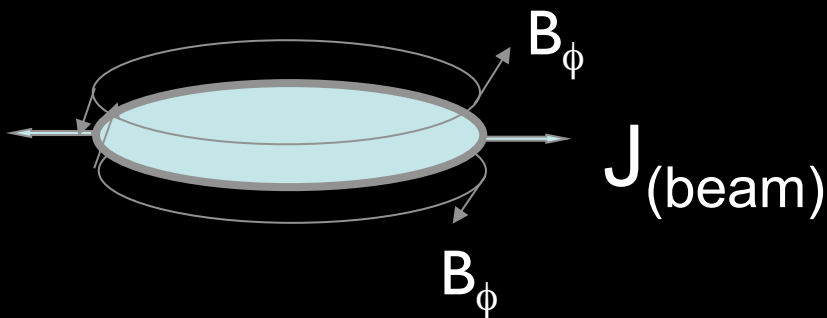


Sironi & Spitkovsky 09

Turbulence too weak, wrong kind (not scattering) to support DSA
in $\langle \sigma \rangle > 0.01$ flow, = latitude average in MHD nebula models

Pulsar Wind Toroidal Field entirely across flow; composition = pairs.
Does shock acceleration fail for best studied/most easily studied
relativistic outflow?

Perhaps/Perhaps not – conclusion applies only if upstream B not
structured – high mass loaded, low Γ_w wind has sandwich geometry



Clue: MHD nebular models require unusually weak field in equator, plasma + beam flow in equatorial current sheet allows formation of $\sigma < 10^{-3}$ shock, Fermi acceleration possible in equatorial outflow: feeds torus, if accel to PeV



(needs turbulence not demonstrated in $\sigma < 10^{-3}$ PIC), spectrum OK for optical, X-ray, gamma ray from nebulae

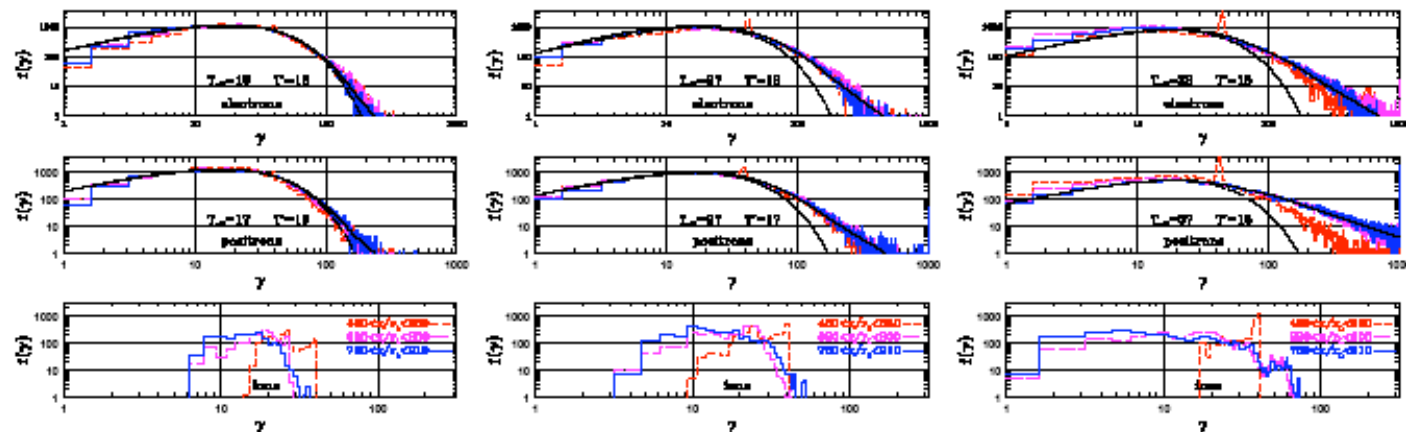
Flat spectrum radio emitters accelerated by cyclotron resonance in higher σ zones at higher latitude?

Amato & JA 1D PIC – hasn't yet been done in 2D and 3D

electrons

positrons

beam= "protons"



Conclusions: Pulsar Problems and Prospects

- ❑ Force Free Currents - Charge Neutrality conflicts with j
New Polar Accelerator Models - short time variability?
- ❑ Closed/Open Magnetosphere - Reconnection?
Cross field transport in closed zone
Plasma transfer from open to boundary layer, closed field - $n < 3$?
Return current formation and plasma E_{\parallel} - kinetic Alfvén waves
Torque noise, subpulse phase variations
Boundary layer acceleration, HE photon emission
Enhanced Polar Pair Creation (?)
- ❑ Wind Current Sheet Dissipation
High $\sigma \rightarrow$ low σ ? Anomalous resistive decay of stripes in mass loaded, low(er) $\Gamma_w \sim 10^4$; Current in equatorial current sheet = runaway beam
- ❑ PWNe termination shocks – Magnetic Sandwich Geometry
unmagnetized in equator (“sandwich filling”): Fermi acceleration (O,X, γ)
cyclotron acceleration at higher latitude: flat radio spectrum?